Timing matters: Tuning the mechanics of a muscle-tendon unit by adjusting stimulation phase during cyclic contractions.

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ABSTRACT

A growing body of research on the mechanics and energetics of terrestrial locomotion has demonstrated that elastic elements acting in series with contracting muscle are critical components of sustained, stable, and efficient gait. Far fewer studies have examined how the nervous system modulates muscle-tendon interaction dynamics to optimize ‘tuning’ or meet varying locomotor demands. To explore the fundamental neuromechanical rules that govern the interactions between series elastic (SEE) and contractile (CE) elements within a compliant muscle-tendon unit (MTU), we used a novel work loop approach that included implanted sonomicrometry crystals along muscle fascicles. This enabled us to de-couple CE and SEE length trajectories when cyclic strain patterns were applied to an isolated plantaris MTU from the bullfrog (Lithobates catesbeianus). Using this approach, we demonstrate that the onset timing of muscle stimulation (i.e., stimulation phase) that involves a symmetrical MTU stretch-shorten cycle during active force production, results in net zero mechanical power output, and maximal decoupling of CE and MTU length trajectories. We found it difficult to ‘tune’ the muscle-tendon system for strut-like isometric force production by adjusting stimulation phase only, as the zero power output condition involved significant positive and negative mechanical work by the CE. A simple neural mechanism- adjusting muscle stimulation phase- could shift a MTU from performing net zero to net positive (energy producing) or net negative (energy absorbing) mechanical work under conditions of changing locomotor demand. Finally, we show that modifications to the classical work loop paradigm better represent in vivo muscle-tendon function during locomotion.

KEY WORDS: muscle-tendon interaction, muscle stimulation phase, work loop, elastic energy storage and return, terrestrial locomotion

SUMMARY STATEMENT: During cyclic contractions of a muscle-tendon unit, the timing of muscle stimulation onset determines whether the muscle acts like a force producing strut, energy generating motor or energy absorbing brake.
INTRODUCTION

During locomotion, skeletal muscles are recruited to generate force and perform a diverse set of mechanical actions (Dickinson et al., 2000). Muscle performance is strongly influenced by its mechanical state and neural activation (Hill, 1925; Hill, 1938; Gordon et al., 1966; Josephson, 1999). The timing and magnitude of activation dictates the context in which muscle forces will generate or absorb mechanical energy (Josephson, 1993, 1999; Ahn and Full, 2002). When activated during a period of shortening, skeletal muscle functions as a motor by performing positive work (Josephson, 1985, 1999; Dickinson et al., 2000). When active during lengthening, however, muscle function as a brake by performing negative work and dissipating mechanical energy (Josephson, 1985, 1999; Dickinson et al., 2000). Finally, within a relatively compliant muscle-tendon unit (MTU), the muscle can be active and isometric (i.e., at constant length) generating high forces to act as a strut while energy is cycled in series elastic elements (Ettema, 1996a; Roberts et al., 1997; Dickinson et al., 2000; Ettema, 2001).

The neuromechanical factors that ultimately determine the amount of force/work produced by active skeletal muscle are its force-length (F-L) and force-velocity (F-V) properties (Hill, 1925; Hill, 1938; Gordon et al., 1966), the magnitude and timing of muscle activation (Josephson, 1985; Stevens, 1996; Dickinson et al., 2000), and environmental factors such as externally applied loads or strain patterns (Josephson, 1985). Sinusoidal length changes similar to those observed during steady locomotion (e.g., walking, running, swimming, flying) provide a useful paradigm for probing how the mechanical state of active muscle ultimately governs cyclic force and power production in a functional task. This sort of ‘work loop’ experiment allows for exploration and understanding of how activation kinetics and F-L/F-V dynamics govern the mode of operation (motor, brake or strut) of a muscle depending on when it is stimulated along its length trajectory (Josephson, 1985, 1999; Ahn, 2012). One limitation of the ‘work loop’ paradigm is the potential inaccuracy when extrapolating from isolated muscles to isolated muscle-tendon units. Length changes applied directly to a muscle-tendon unit (MTU) may not reflect the length and/or velocity of the underlying muscle fascicles (CE); especially if there is considerable series compliance from elastic tissues (SEE). This decoupling can make it difficult to resolve the relative contribution of the CE and SEE to the mechanical behavior of the MTU.

Recent muscle-level studies of terrestrial gait have observed that in the distal, more compliant muscle-tendons of many species including humans, contractile elements (CE) (i.e., active muscle) are in fact used as a strut to allow the series elastic elements (SEE) (i.e., tendon, aponeurosis) within muscle-tendon units (MTU) to stretch and recoil during cyclic limb motions (Roberts et al., 1997; Biewener et al., 1998; Fukunaga et al., 2001; Ishikawa et al., 2005; Takeshita et al., 2006; Dean and Kuo, 2011; Farris and Sawicki, 2012; Farris et al., 2013). In other words, CE length changes are
decoupled from MTU trajectories via SEE compliance, and CE-SEE interaction is ‘tuned’ to cycle large amounts of energy in tendons and aponeuroses while the CE itself remains relatively isometric (Robertson and Sawicki, 2014). This ‘tuned’ pattern facilitates length change dynamics suitable for high CE force production, which in turn, require relatively smaller active volumes of muscle to generate force during each stride (Roberts et al., 1997; Gabaldon et al., 2008).

Our understanding of the patterns of neural control necessary to tune CE and SEE interactions to allow for effective force production is limited. Multiple in-vitro work loop studies exploring the role that tendon compliance plays in gait have relied on mathematical models of the SEE in order to decouple CE/MTU trajectories in the absence of direct muscle level measurements (Ettema et al., 1990; Ettema, 1996a; Lou et al., 1999; Ettema, 2001; Barclay and Lichtwark, 2007; Lichtwark and Barclay, 2010, 2012). For example, Ettema et al. integrated a mathematical model with experimental data to conclude that effective elastic energy storage and release in an SEE is strongly dependent on the timing of muscle stimulation during a MTU stretch-shorten cycle, and that SEE compliance can significantly affect muscle-level energetics without having a dramatic effect on MTU force production (Ettema, 1996a). While there is no doubt that mathematical models of muscle-tendon units provide a useful avenue for examining CE/SEE interaction, they do have limited ability to capture some aspects of the dynamics of force generation in both muscle and tendon. In fact, multiple studies have shown that model-based predictions of muscle force production are flawed for active contractions during non-isokinetic (i.e., variable length/velocity) conditions (Caiozzo and Baldwin, 1997; Sandercock and Heckman, 1997; Lou et al., 1998; Lichtwark and Wilson, 2005). This is further complicated by incomplete models of biological tendon, which do not capture their tendency to dissipate energy over a stretch-shorten cycle (Bennet et al., 1986; Lieber et al., 1991; Maganaris and Paul, 2000).

The purpose of the present study was to use a novel, in vitro muscle-tendon work loop approach to probe how the temporal aspects of neural control influence muscle-tendon interaction within a relatively compliant muscle-tendon unit. We extended the work loop approach by including independent measurements of both muscle fascicle (CE) length and muscle-tendon unit (MTU) length in order to provide data regarding fundamental aspects of muscle-tendon interaction that do not rely on model estimates for CE or SEE force production. Using direct measurements of CE length from sonomicrometry in conjunction with externally applied cyclic length changes via servo controlled ergometer, we examined how the onset timing of muscle stimulation within a MTU length change cycle (i.e., muscle stimulation phase, \( \phi_{stim} \)) relates to the ‘tuned’ muscle-tendon interaction observed within compliant MTUs during steady speed terrestrial gait (Fig. 1). We expected that the relationship between overall MTU net work and muscle stimulation phase, \( \phi_{stim} \), would follow the same trends previously observed in work loop experiments using direct measurements from CE only (Josephson, 1999) and a combination of empirical measures and model-based estimates from whole MTUs (Ettema, 1996a). First, (1) we hypothesized that there would be a muscle stimulation phase, \( \phi_{stim} \),
that would generate net zero work over a MTU length change cycle. We refer to the stimulation phase leading to net zero work as ($\phi_{stim} = \phi_{net\,zero}$). Second, we expected that muscle stimulation with onset that occurred earlier in the MTU length change cycle ($\phi_{stim} < \phi_{net\,zero}$) would generate net negative work while muscle stimulation onset that occurred later in the cycle ($\phi_{stim} > \phi_{net\,zero}$) would generate net positive work. Finally, we expected that the muscle stimulation phase resulting in net zero work for the MTU over a length change cycle ($\phi_{stim} = \phi_{net\,zero}$) would be ‘tuned’, allowing the CE to operate isometrically with all positive and negative work resulting from cycling of elastic energy in the SEE.

RESULTS

All results reported here are taken from trials where cyclic length changes were applied to the muscle-tendon unit (MTU) with a cycle frequency ($\omega_{cycle}$) of 2 Hz (i.e., cycle period =500ms), and an amplitude ($A_{cycle}$) of 4mm with an initial (minimum) MTU length corresponding to a CE length of 1.2$L_0$ (Figs 1, 3).

Peak force.

For all experimental conditions explored, peak force was recorded for each cycle of strain/stimulation (Figs 2, 3), and was averaged within (n=4 cycles) and between (n=6 subjects) preps to determine an average peak force (Fig. 4A). The highest peak force was observed for the 12.5% muscle stimulation phase condition (Figs 2, 4A), and minimum values were recorded for stimulation phase of -37.5% (Fig. 4A). Peak forces were significantly different from 25% phase (Tukey’s; P < 0.05) in the -50%, -37.5%, -25%, and 50% phase and no stimulation conditions (Fig. 4A).

Length change trajectories following muscle stimulation.

All conditions showed significant decoupling of the length change of the CE from that of the MTU (Figs 2, 3). Decoupling was particularly obvious immediately following stimulation; when the rapid rise in force resulted in SEE stretch and significant shortening of the CE, regardless of the direction of length change of the MTU. CE shortening following stimulation onset was observed for all conditions (Figs 2, 3), and was minimal for muscle stimulation phase of 25% (Figs 3D, 4B).

Length change dynamics observed immediately following muscle stimulation onset were of particular interest in this study because it is during this period that active force production tends to decouple MTU trajectory from CE and SEE strain (Fig. 3). All conditions except for 12.5% stimulation phase had active muscle (CE) shortening excursions significantly greater than the 25% stimulation phase condition (Tukey’s; P<0.05) (Fig. 4B). The greatest MTU force output and largest SEE stretch during the period of active CE shortening was observed for the 12.5% phase condition.
(Fig. 4B). SEE strains were significantly less than the 25% phase condition in the 37.5% and 50% conditions (Tukey’s; P<0.05).

Mechanical power output.

We were not only concerned with how force development influenced decoupling of CE/MTU dynamics, but also the role it played in generating mechanical work and power over a stretch shorten cycle. Mechanical power was defined as positive during segment shortening (i.e., positive velocity), and was calculated as the product of force and velocity vs. time as follows:

$$P_{\text{mech}}(t) = F_{\text{MTU}}(t) \times v_{\square}(t)$$

Where $P_{\text{mech}}$ is mechanical power, $v_{\square}$ is velocity, and the $\square$ symbol acts as a placeholder for a subscript of CE, SEE, or MTU depending on the MTU component for which power was computed (Fig. 5).

In every dynamic condition, onset of muscle stimulation was followed by rapid force development, shortening, and positive power production by the CE, regardless of whether the MTU was shortening or lengthening. During MTU lengthening, positive power production by the CE was associated with negative power (energy storage) from the SEE. Energy stored in the SEE has two possible fates. It can be returned externally to the motor, as positive MTU power, or it can do work on the CE to lengthen active muscle fibers. The extent to which work done by the CE on the SEE could be returned externally varied, depending on the phase of stimulation (Fig. 5). Under some conditions (e.g., 0% phase), all of the energy stored in the SEE was released to do work on the CE, rather than contribute to MTU power.

Decoupling of CE and MTU mechanics.

Because we expected there to be some decoupling between CE and whole MTU length change dynamics, we computed a Pearson product-moment correlation coefficient to compare time averaged CE and MTU velocities over a stretch shorten cycle. $r$ values were computed as follows:

$$r = \frac{\sum_{n=1}^{N}(v_{CE}^n - \bar{v}_{CE})(v_{MTU}^n - \bar{v}_{MTU})}{\sqrt{\sum_{n=1}^{N}(v_{CE}^n - \bar{v}_{CE})^2} \sqrt{\sum_{n=1}^{N}(v_{MTU}^n - \bar{v}_{MTU})^2}}$$

Where the coefficient $n$ corresponded to a single discrete sample within a given period, $N$ is the total number of samples recorded over a stretch-shorten cycle ($T_{\text{cycle}} = 500$ ms, sample rate = 1000Hz, $N=500$ for all data presented here), and $\bar{v}_{CE}$ and $\bar{v}_{MTU}$ are the average muscle (CE) and muscle-tendon unit (MTU) velocities, respectively, over a stretch-shorten cycle. A value of 1 indicates a perfect correlation, 0 is completely uncorrelated, and -1 indicates perfect inverse correlation. We note, that although this approach serves well in the current study as a simple way to quantify the relative amount of decoupling between MTU and CE dynamics, it may not generalize to situations that are not as highly controlled in terms of the frequency and amplitude of the overall MTU length change, timing.
of the muscle stimulation phase and regularity of the data sampling frequency. For example, when comparing signals that may have variation in sampling frequency, the correlation coefficient is prone to errors resulting from clustering of data in certain regions of the curves that could bias the measure.

\( r \) values computed based on CE vs. MTU velocities were between 0 and 1 (i.e., positively correlated) for all conditions examined (Fig. 6). A minimum average \( r \)-value of 0.09 was observed for the 25% phase condition (Fig. 6B), which was significantly lower than all other stimulation phase conditions except for 12.5% (Tukey’s \( P<0.05 \)) (Fig. 6D).

**Net, positive, and negative mechanical work.**

To examine how the muscle stimulation phase influenced average positive, negative, and net mechanical work produced over a stretch-shorten cycle for the muscle-tendon (MTU) and its components (CE, SEE) we computed:

\[
W_{\text{mech}} = \int_{t=0}^{T_{\text{cycle}}} P_{\text{mech}}(t) \, dt
\]

Where \( W_{\text{mech}} \) was net mechanical work over a full MTU stretch shortening cycle, starting with \( t=0 \), the time of muscle stimulation onset and ending at \( T_{\text{cycle}}=500\text{ms} \) later (Fig. 1); and \( \Box \) was a placeholder for either CE, SEE or MTU subscripts. To compute positive and negative work over a cycle, we simply integrated only the positive or negative region of instantaneous mechanical power curve. Holding with convention from previous literature, we have defined positive work as mechanical energy produced, while negative work indicates energy absorbed by the element of interest.

The MTU produced approximately zero net work with onset of muscle stimulation at 25% of the MTU length change cycle (i.e., \( \phi_{\text{stim}} = \phi_{\text{net zero}} = 25\% \)) (Figs 3F, 5H, 7A). Because net work over the course of an entire MTU length change cycle must be due to the CE, net work in the CE and MTU were nearly identical in all muscle stimulation phase conditions (Fig. 7A). Even in the condition with nearly zero net work (i.e., \( \phi_{\text{stim}} = \phi_{\text{net zero}} = 25\% \)), we did not observe ‘tuned’, strut-like isometric behavior of the CE. Instead, in the 25% stimulation phase condition the CE underwent significant length change following stimulation (Figs 3D, 4B) and thus generated and absorbed significant but equal amounts of mechanical energy (Figs 5H, 7B, C).

When muscle stimulation onset occurred earlier in the MTU length change cycle than for conditions of net zero work (\( \phi_{\text{stim}} < \phi_{\text{net zero}} = 25\% \)), the MTU and CE generated net negative work (Figs 3C, 5G, 7A). Maximal energy absorption by the MTU and CE occurred for the 0% stimulation phase condition. Muscle stimulation phases ranging from -12.5% to +12.5% of the MTU length change cycle generated significantly more net negative CE and MTU work than the 25% condition (Tukey’s; \( P<0.05 \)) (Fig. 7A). We note, as expected, SEE net work was small and ~zero or negative for all conditions studied here because passive tissues can only store and return mechanical energy with small losses (Fig. 7A).
When muscle stimulation had onset that occurred later in the MTU length change cycle than for conditions of net zero work ($\phi_{stim} > \phi_{net\ zero} = 25\%$), the MTU and CE generated net positive work (Figs 3I, 5I, 7A). Maximal net positive MTU and CE work per cycle was observed for the 50% muscle stimulation phase condition, however, none of the conditions generated net positive work that was significantly different from the 25% condition (Tukey’s; $P \geq 0.05$) (Fig. 7A).

**DISCUSSION**

While the mechanical roles of elastic elements during terrestrial gaits are well understood, the role that neural control plays in governing them is not. Therefore, we employed a novel *in vitro* MTU work loop approach to determine how MTU, CE and SEE mechanics are modulated by the timing of muscle stimulation within a cyclical MTU strain trajectory (*i.e.*, muscle stimulation phase). We specifically focused on elucidating the role of neural control in shaping muscle-tendon interaction dynamics for the condition of zero net MTU work, conditions akin to steady speed terrestrial locomotion.

We hypothesized that (1) there would be an onset timing of muscle stimulation relative to the muscle-tendon unit (MTU) length change cycle that resulted in net zero MTU work over a stretch shorten cycle ($\phi_{stim} = \phi_{net\ zero}$); and that (2) muscle stimulation timed earlier ($\phi_{stim} < \phi_{net\ zero}$) would result in net negative MTU work, while muscle stimulation timed later ($\phi_{stim} > \phi_{net\ zero}$) would result in net positive MTU work. Our data supported these hypotheses (Fig. 7A). We note that, despite significant decoupling of muscle fascicle (CE) and whole MTU dynamics observed here (Fig. 6), $\phi_{net\ zero}$ for a compliant MTU occurred at a similar muscle stimulation phase as has been previously observed for isolated muscles without significant series elastic tissues (Josephson, 1985, 1999).

Our final hypothesis was that, (3) the muscle stimulation phase resulting in net zero work ($\phi_{stim} = \phi_{net\ zero}$) would be ‘tuned’ so that all positive and negative work produced by the MTU would be the result of elastic energy storage and return in the SEE, with little to no positive/negative mechanical work output from active muscle (CE). This hypothesis was not supported as the CE produced non-negligible amounts of both positive and negative work over a stretch shorten cycle for the $\phi_{stim} = \phi_{net\ zero} \sim = 25\%$ condition (Fig. 7B).

*A coordination rule for net zero work: Aligning active muscle force with symmetric MTU stretch-shortening.*

Under conditions specific to this study (*i.e.*, MTU length change cycle duration = 500ms, muscle stimulation duration = 50ms) we found that an onset of muscle stimulation (*i.e.*, stimulation phase) of $\sim 25\%$ resulted in net zero MTU work over a cycle ($\phi_{net\ zero} = 25\%$). To begin to generalize
our findings beyond the specific conditions of this study, we observed the force and length change dynamics of the MTU with respect to muscle stimulation timing (Figs 3D, E) and devised a qualitative rule for zero net work as follows: Employ stimulation timing and duration so that there is a symmetrical MTU lengthen-shorten cycle during the period of active muscle force production. These conditions can be summarized mathematically by a simple equation relating the onset of muscle stimulation (i.e., stimulation phase) that yields net zero work ($\phi_{\text{net, zero}}$) to the duration of active muscle force production ($D_{\text{force}}$) for a given stimulus pattern, both expressed as a percentage of the MTU length change cycle period.

$$\phi_{\text{net, zero}} = 50 - 0.5 \times D_{\text{force}}$$

In this formulation, 0% phase is the time of minimum MTU length (i.e., ergometer bottom dead center) and 50% phase is the time of peak MTU length (i.e., ergometer top dead center) (Fig. 1). For the experiments presented here, 50ms of muscle stimulation resulted in a duration of active muscle force of ~250ms (Fig. 2). Since the cycle period for a 2Hz MTU length change pattern is 500ms (Fig. 1), the duration of active muscle force production as a percentage of the length change cycle period, $D_{\text{force}}$, was ~250ms/500ms *100 or 50%. Using Eq. 4, $D_{\text{force}} =$50% yields an estimate for the onset of muscle stimulation timing (i.e., stimulation phase) that would lead to net zero MTU work over the cycle; $\phi_{\text{net, zero}} =$25%. This estimate is in good agreement with the experimental observation of net zero MTU work (Fig. 7A) in this study, as the 25% stimulation phase condition aligns active force onset/offset with MTU lengthening/shortening (Figs 3, 5) to facilitate effective elastic energy storage/return in the SEE (Figs 3, 5, 7B-C) and net MTU mechanical power output of ~0 (Fig. 7A).

We expect that this relationship (Eq. 4), albeit very simple, could provide a useful initial framework for relating neural control (stimulation amplitude, phase and duty) and mechanics of muscle-tendon systems during cyclic contractions. Future work will focus on elucidating the influence of sub-maximal muscle activation and muscle-tendon architecture on $D_{\text{force}}$ to expand the utility of Eq. 4 to conditions even closer to ‘real-world locomotion.

**Challenges of achieving ‘tuned’ isometric force production in muscle-tendon systems.**

During steady speed terrestrial locomotion, compliant muscle-tendons at distal joints (e.g., the ankle) cyclically lengthen and shorten from step to step. This creates an opportunity for optimally coordinating muscle activation timing and amplitude to ‘tune’ muscle-tendon interaction for maximal performance. For example, if muscles are activated with timing and amplitude that supplies a rigid force producing strut (i.e., ’tuned’ to be nearly isometric), they can allow elastic tissues to stretch and recoil during limb segment lengthening and shortening in order to cycle the energy required for steady gait. Due to the intrinsic force-length and force-velocity relationships, strut-like muscle-level dynamics are particularly well suited for high force production, reducing the volume of active muscle...
required to meet force demands, and ultimately increasing the economy of locomotion (Roberts et al., 1997; Gabaldon et al., 2008).

Our results suggest that, even in the presence of highly compliant elastic tissues in series with muscle fascicles, tuning the CE for strut-like force production (i.e., near isometry) during cyclic contractions is challenging. Contrary to our third hypothesis, the net zero work condition ($\phi_{\text{net zero}} = 25\%$) resulted in significant length changes of the CE. That is, the net zero work condition was accomplished not by isometric force production by the CE, but by significant and approximately equal amounts of positive and negative work (Fig. 7B-C). Shortening work occurred early in the period of force production, as the CE shortened against the SEE, and lengthening work occurred when the SEE recoiled against the CE. While this pattern represented the most decoupled CE/MTU behavior (Fig. 6), this behavior was far from the “ideal” of an isometric CE strut supporting the cyclic stretch and recoil of tendon.

Why is isometric muscle behavior difficult to achieve under the conditions of our experiment? One likely issue is the combination of asymmetric muscle activation/deactivation dynamics (Zajac, 1989), and a symmetric/sinusoidal strain pattern. In general, muscle force onset occurs more rapidly than offset (Fig. 2). When symmetric patterns of MTU strain are applied to a muscle with asymmetric force onset/offset, some muscle shortening/lengthening is going to be required to match passive forces in series elastic tissues (SEE). One possible approach to addressing this asymmetric force output is to apply an asymmetric strain pattern. Marsh and coworkers have demonstrated that when asymmetric strains are applied, it is possible to maximize power output from muscle alone (Askew and Marsh, 1997; Girgenrath and Marsh, 1999). With this in mind, we attempted to design an ergometer controller that would apply the required MTU strain pattern to keep CE length constant during muscle activation/deactivation using real-time sonomicrometry measurements as feedback (Sawicki and Roberts, 2009). The resulting MTU strain pattern was highly asymmetric and the length of the CE remained more isometric than shown in the current study. However, it was still not possible to achieve ‘perfect’ isometry as we could not avoid internal CE shortening against the SEE early in the supramaximal contractions of the compliant MTU. We note that animals likely use dynamically changing moment arms (Carrier et al., 1994) and pennation angles (Azizi et al., 2008), combined with differential sub-maximal motor-unit recruitment patterns (Holt et al., 2014) that can be modulated by reflex feedback (Maas and Lichtwark, 2009) to help ‘dial in’ nearly perfect strut-like muscle action during real-world locomotion.

**Modulating muscle stimulation phase to meet changing mechanical demands during locomotion?**

Gait on level ground at constant speed requires no net mechanical work, but most terrestrial animals experience terrain that imposes varying mechanical demands (e.g., slowing down, speeding up, going up/downhill). The decoupling of MTU and CE by SEE may afford considerable advantages during unsteady locomotion including (1) limiting negative work absorbed by CE when
active during MTU lengthening (Roberts and Azizi, 2010), (2) amplifying positive work by allowing muscle to operate at velocities for optimal power output during MTU shortening (Lichtwark and Barclay, 2010) and (3) providing a rapid means of mechanical feedback (i.e., ‘preflex’) following environmental perturbation (Daley and Biewener, 2006; Biewener and Daley, 2007). Our results support previous research suggesting that locomotion tasks involving net generation or absorption of mechanical energy may be accessible by adjusting timing of muscle stimulation relative to the pattern of MTU strain (Ettema, 1996a, 2001; Lichtwark and Wilson, 2005; Lichtwark and Barclay, 2010, 2012). We observed that slight changes in muscle stimulation onset phase from the $\phi_{\text{net zero}}$ (i.e., 25% ±12.5%) resulted in near maximal values of net positive/negative work respectively (Fig. 7A).

Our data are consistent with previous studies by Ettema et. al. (Ettema, 1996a) and Lichtwark et. al. (Lichtwark and Barclay, 2010), which varied frequency, phase, and stimulation duty in a compliant MTU. Both of these studies emphasized the importance of proper muscle stimulation timing to either effectively store and return energy in series tendon (Ettema, 1996a), or maximize efficiency in shortening for performing positive work (Lichtwark and Barclay, 2010). Shifting muscle activation phase could provide a potentially simple neural mechanism for altering compliant MTU function to produce net negative (braking or moving downhill), net zero (constant speed), or net positive (acceleration or moving uphill) mechanical work output.

Benefits of direct muscle-level measurements in MTU work loop experiments.

The most novel aspect of this study was the use of implantable sonomicrometry for direct measurement of muscle-level mechanics during dynamic work loop experiments. Previous work loop studies of MTU mechanics have relied on model based approximations of SEE force-length behavior to dissect CE from SEE length changes. Ettema left the biological SEE intact, approximated SEE stiffness under high force conditions, and assumed perfect elasticity (i.e., all energy stored in SEE must be returned) to calculate the contribution of the SEE (Ettema et al., 1990; Ettema, 1996a, b). Multiple studies, however have demonstrated that biological tendon exhibits non-linear force-length behavior at low strains (Lichtwark and Wilson, 2007), and that volumetric changes in active muscle can change elastic properties of aponeurosis/SEE (Azizi and Roberts, 2009). Tendon will also dissipate some energy over a stretch-shorten cycle (Fig. 7A) (Bennet et al., 1986; Lieber et al., 1991; Maganaris and Paul, 2000). Lichtwark and Barclay avoided many of these pitfalls by removing tendon all-together, and replacing it with elastic strips of latex with well-defined linear stiffness (Lichtwark and Barclay, 2010, 2012). While this is an excellent approach to studying the effect of series compliance on muscle level function, it is missing many of the aforementioned mechanical features of biological tendon that might have a subtle but significant impact on CE mechanics. That being said, findings presented here confirmed previous experimental observations of Litchwark et al. without the need for any sort of model based approximation and further highlight that SEE compliance can have a profound impact on CE contractile dynamics.
Limitations of the classical work loop approach and future directions.

While work loops have proven an effective means of exploring how strain trajectories and neural activation influence muscle-level mechanics and energetics (Ahn, 2012), they depart from muscle function during ‘real-world’ locomotion in significant ways (Marsh, 1999). During locomotion, muscle strain trajectories are not a pre-existing phenomenon to which neural activation patterns can be applied. Rather, they are an emergent behavior resulting from active muscle force, transmitted through mechanical lever systems (i.e., biological moment arms), and interaction with an inertial-gravitational load (Marsh, 1999; Richards and Clemente, 2012; Robertson and Sawicki, 2014). To understand the dynamic interplay of all of these factors, and the role that they play in generating stable/efficient MTU mechanics observed in gait, trajectory must not be imposed (Robertson and Sawicki, 2014).

During locomotion in the ‘real-world’, the dynamic interactions between muscle-tendons of the limb and the load of the body serve to couple muscle stimulation frequency and phase. Thus, future work should focus on simulating a dynamic inertial environment (i.e., mechanical advantage, gravitational load) that can freely interact with a biological MTU undergoing cyclic stimulation (Sheppard et al., 2009; Farahat and Herr, 2010; Robertson and Sawicki, 2014). With direct, real-time measurements of both fascicle level dynamics via sonomicrometry and muscle force from the ergometer as we have done in the current study, we could simulate spindle organ (i.e., length/velocity) and/or golgi tendon (i.e., force) afferent feedback. By varying muscle stimulation intensity (via rate-coding) as a function of simulated feedback within and between muscle stimulation pulses it may be possible to begin systematically exploring how environment dynamics, as well as feed-forward and feed-back neural control processes (e.g. reflexes) govern the influence of muscle activation on the mechanics and energetics of muscle-tendon interaction (Stevens, 1996; Farahat and Herr, 2010; Richards and Clemente, 2012).

MATERIALS AND METHODS

Experimental Preparation

Animal subjects.

Six adult bullfrogs (Lithobates catesbeianus), with body masses ranging from 214-373g, were purchased from a licensed vendor and housed in the Brown University Animal Care facility in a large tank of shallow water with free access to a terrestrial platform. Subjects were fed large, vitamin enriched crickets ad libitum twice weekly. Before use in experimental procedures, animals were given a minimum acclimation period of 1 week. Prior to their use in any experimental preparation, frogs were anesthetized and euthanized via double pithing. All animal procedures were approved by Brown University Institutional Animal Care and Use Committee.
In-vitro preparation.

A single limb from each subject was removed just below the hip, skin was removed, and the limb was placed in a bath of oxygenated amphibian Ringer’s solution (100 mM NaCl, 2.5 mM KCl, 2.5 mM NaHCO₃, 1.6 mM CaCl₂, 10.5 mM Dextrose) and kept at room temperature (~22°C) during dissection. All muscles were completely removed except the plantaris longus (PL) muscle-tendon unit, which serves as the primary ankle extensor, and is known to be both compliant (i.e., high ‘fixed-end’ compliance and SEE/MTU length ratio), and a major source of power output during jumping. Caution was taken during removal of proximal muscles to ensure the sciatic nerve remained intact. The PL muscle was left intact at its proximal insertion point (the knee joint), and freed from the ankle and tibiafibula, with great care taken to preserve series aponeurosis and free tendon up to its distal insertion point at the toes.

Following dissection, a bipolar electrode cuff constructed from two silver wires and plastic tubing (7mm length, 1.5mm inner diameter) was carefully placed over the free (but intact) sciatic nerve just proximal to the PL insertion point at the knee and connected to a Grass S48 stimulator (Grass Technologies, West Warwick, RI, USA). Sonomicrometry transducers (1 mm diameter, Sonometrics Inc., London, Ontario, CA USA) were implanted along a superficial, proximal muscle fascicle of the PL muscle and sutured in place to provide direct measurement of fascicle (CE) length change (i.e., decoupled from whole muscle-tendon unit (MTU) length change) (Fig. 1).

Intact sections of femur and tibia were securely mounted on acrylic bolted at the bottom of a chamber with continuously circulating oxygenated Ringer’s solution maintained at room temperature (22°C). The distal end of the free tendon was placed in a custom friction clamp attached to a servomotor (310 B-LR, Aurora Scientific Inc., Cambridge, MA, USA) via rigid stainless steel cable (stiffness=~94.1 N/mm) (Fig. 1).

Measurement of muscle-tendon unit (MTU), muscle fascicle (CE) and elastic tissue (SEE) force, length, velocity and mechanical power.

Muscle-tendon unit (MTU) force and length were recorded from the servomotor and muscle fascicle length (CE) was recorded using sonomicrometry (Fig. 1) and a 16-bit A/D converter (National Instruments USB- 6251, Austin, TX, USA) sampling at 1000 Hz. Data were processed and analyzed using custom Matlab software (Mathworks Inc., Natick, MA, USA). Raw data (MTU force, MTU length, muscle fascicle (CE) length) were smoothed using a 4th order Butterworth, zero lag filter with low pass cutoff frequency of 25 Hz. In all trials, we subtracted the length change of the stainless steel cable connecting the ergometer and the MTU, by subtracting 1/94.1 mm/N of force to get the true length change of the MTU.

To compute the velocity of the MTU and the CE we took the first derivative of the smoothed servomotor and sonomicrometry length change data, respectively. The length change and velocity of
the series elastic tissues (SEE) was computed by simply subtracting the CE from the MTU length/velocity, respectively (e.g., Figs 2, 3, 5). We note, that this approach implies that 
\[ \Delta L_{MTU}(t) = \Delta L_{CE}(t) + \Delta L_{SEE}(t) \] and 
\[ v_{MTU} = v_{CE}(t) + v_{SEE}(t) \]
which assumes that fascicles (CE) and elastic tissues (SEE) reside along the same geometrical axis as the whole MTU. Finally, we computed mechanical power (mW) by multiplying instantaneous MTU force (N) and velocity (mm/s) for the MTU and each of its component parts (i.e., CE and SEE; e.g., Fig. 5). We note, that because fascicles rotate while they shorten/lengthen and we did not record fascicle pennation angle, we could not estimate length changes of the CE along the MTU/SEE long axis. As a result, our length change measurements using sonomicrometry crystals implanted in fascicles are likely an underestimate of the CE length change along the MTU/SEE long axis (Azizi et al., 2008; Azizi and Roberts, 2014). These underestimates in CE length change and velocity will lead to overestimates in calculated SEE length change and velocity and therefore tend to attribute too much MTU mechanical power to the SEE and too little to the CE.

Estimation of muscle rest length, \( L_0 \), for calculating dynamic strain.

Normalized CE strains reported throughout (e.g., Figs 2,3) are based on the absolute length at which the muscle developed 1N of passive tension, and previous experimental observation that this passive force occurs at a CE length of 1.2\( L_0 \), so that

\[ L_0 = \frac{L_{F=1}}{1.2} \]

Where \( L_0 \) is the length at which isometric muscle produces peak active forces, \( L_{F=1} \) is the absolute length of the CE under 1N of passive force, and 1.2 is the strain at which bullfrog muscles of similar size develop a passive force of 1N (Azizi and Roberts, 2010).

‘Fixed-end’ contractions.

Prior to any dynamic work loop conditions, ‘fixed-end’ contractions were performed by holding ergometer position constant to impose a MTU length that resulted in 1N of passive tension (CE length = ~1.2\( L_0 \)), and then applying 4 stimulation trains at a frequency (\( \omega_{stim} \)) of 2 Hz with a duty factor (\( D_{stim} \)) of 10\% (i.e., 50ms). Each stimulation train consisted of pulses with a duration (\( t_{pulse} \)) of 0.2 ms and a pulse frequency (\( \omega_{pulse} \)) of 100Hz. The average peak force from the 4 ‘fixed-end’ contractions was recorded. Data showing a snapshot of a typical ‘fixed-end’ trial is shown in Fig. 2. The small amount of MTU shortening in these trials reflects the fact that we accounted for the ~0.011 mm/N of compliance of the stainless steel cable used to attach the distal tendon to the ergometer arm. We note that the amount of muscle strain against internal stretch of the series elastic tissues, or ‘fixed-end’ compliance of this preparation was ~0.30, in line with the value reported for the human gastrocnemius muscles (Narici et al., 1996; Biewener and Roberts, 2000;
Roberts, 2002), indicating that the bullfrog plantaris is a convenient scaled down model for human plantarflexors.

A second set of ‘fixed-end’ contractions was performed at the conclusion of all dynamic work loop conditions. Peak force values from the second set of ‘fixed-end’ contractions were compared to those for the first to be sure that muscle fatigue or damage due to trauma or low-levels of oxygenation in deep portions of the tissue did not play a significant role in observed dynamics. For the six experimental preparations reported, the final peak force was ≥80% of the initial value, so factors negatively impacting force production were considered to be a non-factor, and data was used for further analysis.

**Work loop experiments.**

Cyclic length changes were applied to the MTU with a cycle frequency ($\omega_{\text{cycle}}$) of 2 Hz (i.e., cycle period $=500\text{ms}$), and an amplitude ($A_{\text{cycle}}$) of 4mm with an initial (minimum) MTU length corresponding to a CE length of $1.2L_0$ (Figs 1, 3). The MTU prep was placed through 6 cycles of shortening and lengthening, with the first and last cycle occurring in the absence of any muscle stimulation (Fig. 3). For the middle four cycles, muscle stimulation was driven via direct nerve stimulation with a specified onset timing that was different in each condition. More specifically, we defined the onset timing of muscle stimulation (i.e., muscle stimulation phase) with respect to the MTU length change cycle, with 0% referring stimulation onset at MTU minimum length (i.e., ‘bottom dead center’), and 50% referring to MTU maximum length (i.e., ‘top dead center'). We tested muscle stimulation phases ranging from -37.5% to 50% in 12.5% increment, always using a 50ms pulse train duration (i.e., duty factor, $D_{\text{stim}}=10\%$) (Fig. 1). Stimulation was delivered in a pulse train with each individual pulse having period $t_{\text{pulse}} = 0.2\text{ms}$, and pulses delivered with frequency $\omega_{\text{pulse}} = 100\text{Hz}$. The order of muscle stimulation phase conditions was randomized in all *in-vitro* preparations to minimize fatigue effects on averaged data.

**Statistical analysis.**

To determine the influence of muscle stimulation phase on observed muscle-tendon mechanical performance, a two-factor analysis of variance (ANOVA) with subject (i.e., repeated measures) and muscle stimulation phase as the independent variables. We performed ANOVA analyses for all dependent variables of interest (Figs 4A-B; 6D, and 7A-D), with $\alpha = 0.05$. For dependent variables where we found a significant main effect ($p < 0.05$), we report results from a post-hoc Tukey’s’ honestly significant difference (HSD) test indicating which conditions were significantly different ($p<0.05$) from the 25% muscle stimulation phase condition. All values are reported as mean ± S.E.M.
LIST OF SYMBOLS AND ABBREVIATIONS

MTU  muscle tendon unit
SEE  series elastic element, or tendon and aponeurosis
CE   contractile element, or muscle fascicles
$L_0$ muscle fascicle rest length
$\omega_{cycle}$ frequency of the sinusoidal muscle-tendon unit length change cycle
$A_{cycle}$ amplitude of the sinusoidal muscle-tendon unit length change cycle
$\phi_{stim}$ muscle stimulation phase, or, time of muscle stimulation onset expressed as a % of the muscle-tendon unit length change cycle with 0% representing minimum and 50% representing maximum length, respectively.
$\phi_{net\,zero}$ muscle stimulation phase that generates net zero muscle-tendon mechanical work
$D_{stim}$ stimulation duty factor, % of a muscle-tendon unit length change cycle period that stimulus pulse train is ‘on’
$D_{force}$ active force duty factor, % of a muscle-tendon unit length change cycle period when the muscle is actively producing force
$t_{pulse}$ duration of each individual pulse within a stimulus pulse train
$\omega_{pulse}$ frequency of individual pulses within a stimulus pulse train

AUTHOR COMPETING INTERESTS

The authors declare no competing interests.

AUTHOR CONTRIBUTIONS

GSS and TJR conceived of the study; GSS, EA and TJR constructed the experimental apparatus and designed the experimental protocol; GSS and EA carried out experiments, GSS and BDR analyzed the data, GSS and BDR drafted the manuscript, GSS, BDR, EA and TJR edited the manuscript. All authors gave final approval for publication.

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REFERENCES


Table 1: MTU architecture parameters. Mean ± standard error of the mean (S.E.M) for muscle tendon architecture parameters recorded for the six bullfrog plantaris muscle-tendon preparations used in this study. Muscle mass (g) is the dry mass of the muscle belly and aponeurosis without the free-tendon. $L_0$ is the estimated rest length of the fascicles instrumented with sonomicrometry crystals (see Methods). $L_{FT}/L_{MTU}$ is the ratio of the free-tendon length to the whole muscle-tendon unit length. Note that fascicle $L_0$ is not merely the difference between $L_{MTU}$ and $L_{FT}$ because there is significant aponeurosis and fascicle pennation.

<table>
<thead>
<tr>
<th>PARAMETER (N=6)</th>
<th>MEAN ± S.E.M.</th>
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<tbody>
<tr>
<td>Muscle mass (g)</td>
<td>3.54 ± 0.48</td>
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<tr>
<td>$L_0$ (mm)</td>
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<tr>
<td>Muscle-tendon length (mm)</td>
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<tr>
<td>Free-tendon length (mm)</td>
<td>31.10 ± 2.1</td>
</tr>
<tr>
<td>$L_{FT}/L_{MTU}$ (unitless)</td>
<td>0.43 ± 0.01</td>
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Figure 1: Schematic of MTU work loop experimental apparatus and protocol. A) Schematic of experimental muscle-tendon unit work loop preparation. A bullfrog plantaris muscle-tendon unit (MTU) was attached using an aluminum clamp and steel cable to an ergometer and driven through sinusoidal length change cycles while an electrical stimulus was applied to the sciatic nerve over set time periods during a cycle. Sonomicrometry was used to directly measure the length change of the
muscle fascicles (CE) within the muscle-tendon unit (MTU). **B)** Schematic showing the imposed muscle-tendon unit (MTU) length change trajectory (frequency 2 Hz, amplitude 4 mm, positive is lengthening) (green) and the set of conditions for onset timing and duration of muscle stimulation (orange) explored in this study. The onset timing of muscle stimulation (*i.e.*, muscle stimulation phase) was defined with respect to the MTU length change cycle, with 0% referring to MTU minimum length (*i.e.*, ‘bottom dead center’), and 50% referring to MTU maximum length (*i.e.*, ‘top dead center’). We tested muscle stimulation phases spanning from -37.5% to +50% and stimulus always had a 50ms duration (*i.e.*, 10% duty) (orange).
‘Fixed-End’ Contractions

A) Length change of muscle-tendon unit (MTU, green), muscle fascicles (CE, red) and series elastic tissues (SEE, blue) vs. time, starting with muscle stimulation onset. Left axis is absolute length and right axis is strain with respect to fascicle rest length $L_0$.

B) Force vs. time. The orange bar under this axis indicates onset/offset and duration (50ms) of the applied electrical stimulation.

C) Work loop dynamics observed in a typical ‘fixed-end’ contraction. Note significant internal shortening/lengthening of CE and SEE respectively when CE is activated and MTU length is held constant.

Figure 2: Data snapshot from a typical ‘fixed-end’ contraction cycle. A) Length change of muscle-tendon unit (MTU, green), muscle fascicles (CE, red) and series elastic tissues (SEE, blue) vs. time, starting with muscle stimulation onset. Left axis is absolute length and right axis is strain with respect to fascicle rest length $L_0$. B) Force vs. time. The orange bar under this axis indicates onset/offset and duration (50ms) of the applied electrical stimulation. C) Work loop dynamics observed in a typical ‘fixed-end’ contraction. Note significant internal shortening/lengthening of CE and SEE respectively when CE is activated and MTU length is held constant.
Figure 3: Work loop dynamics for the MTU, CE and SEE across stimulation phase. Cyclic contraction dynamics observed for muscle stimulation phase of A-C) 0%, D-F) +25%, and G-I) +50%. Each condition was placed through six cycles of muscle-tendon unit shortening/lengthening. Plots of length change, Δ length (left axis) and CE strain (right axis) vs. time (A, D, G), force vs. time (B, E, H) and torque vs. time (C, F, I).
(B, E, H), and average work loop dynamics (force vs. Δ length) (C, F, I) for stretch/shorten cycles where stimulation was applied are shown for each condition. Dynamics for the muscle-tendon unit (MTU, green), the muscle fascicles (CE, red) and the series elastic tissues (SEE, blue) are displayed where appropriate. Orange bars beneath plots of force vs. time (B, E, H) indicate timing (i.e., phase) and duration (duty=10% or 50ms) of muscle stimulation. Note that electrical stimulation is only applied in the middle 4 cycles, with the first and last stretch/shorten cycles occurring in the absence of stimulation (i.e., passively). Work loops traveling clockwise generate net negative work over a cycle (e.g., CE and MTU with muscle simulation phase=0% (C)); work loops traveling counter clockwise generate net positive work over a cycle (e.g., CE and MTU with muscle simulation phase=50% (I)).
Figure 4: MTU component force and length change vs. stimulation phase. A) Mean peak force observed during active stretch shorten cycles for all muscle stimulation phase conditions (left) as well as no stimulation (i.e., passive length change) and ‘fixed-end’ conditions (i.e., no muscle-tendon unit length change, right). B) Mean length change observed from the onset of muscle stimulation to the end of active muscle fascicle (CE) shortening for the muscle tendon unit (MTU, green), muscle fascicles (CE, red) and series elastic tissues (SEE, blue). Negative is shortening. Values significantly different (Tukey’s; p<0.05) from the +25% phase condition are indicated by a * for MTU, † for CE, and § for SEE. Values presented are ± one S.E.M.
Figure 5: MTU component force, velocity and power vs. time across stimulation phase. A-C) Force vs. time for the 0% (A), +25% (B), and +50% (C) muscle stimulation phase conditions (left to right). The orange bar indicates the timing and duration of electrical stimulation. D-F) Velocity vs. time for the 0% (D), 25% (E), and 50% (F) muscle stimulation phase conditions. Positive is shortening. G-I) Mechanical power vs. time (s) for the 0% (G), +25% (H), and +50% (I) muscle stimulation phase conditions. Velocity and mechanical power are shown for the whole muscle tendon unit (MTU, green) the muscle fascicles (CE, red) and the series elastic tissues (SEE, blue). Note that in all conditions, muscle stimulation onset results in significant muscle fascicle (CE) shortening/mechanical power generation while the series elastic tissues (SEE) lengthen/absorb mechanical energy to varying degrees.
Figure 6: Decoupling of MTU and CE length change dynamics. A-C) Muscle-tendon unit velocity ($v_{MTU}$) vs. muscle fascicle velocity ($v_{CE}$) for the 0% (A), +25% (B), and +50% (C), muscle stimulation phase conditions. The dashed diagonal line indicates a trajectory where $v_{CE} = v_{MTU}$. D) Mean Pearson product-moment correlation coefficient ($r$) value comparing instantaneous MTU and CE velocities. Lower $r$ values indicate greater degree of decoupling between MTU and CE length change trajectories. The * symbol indicates an $r$ value significantly different (Tukey’s; $p<0.05$) from that observed for the +25% stimulation phase condition.
Figure 7: MTU component net, positive and negative work vs. stimulation phase. A-C) Mean ± standard error of the mean (S.E.M.) for net (A), positive (B), and negative (C) mechanical work performed over a full stretch-shorten cycle for the muscle-tendon unit (MTU, green), muscle fascicles (CE, red) and series elastic tissues (SEE, blue). Net MTU work output shifts from absorption to generation as muscle stimulation phase increases from -25 to +50%. Mechanical work values significantly different (Tukey’s; p<0.05) than those observed in the +25% muscle stimulation phase condition are marked with a * for MTU, a † for CE, and § for SEE.