STATIC FORCES AND MOMENTS GENERATED IN THE INSECT LEG: COMPARISON OF A THREE-DIMENSIONAL MUSCULO-SKELETAL COMPUTER MODEL WITH EXPERIMENTAL MEASUREMENTS

R. J. FULL AND A. N. AHN

Department of Integrative Biology, University of California at Berkeley, Berkeley, CA 94720-3140, USA

Accepted 3 February 1995

Summary

As a first step towards the integration of information on neural control, biomechanics and isolated muscle function, we constructed a three-dimensional musculo-skeletal model of the hind leg of the death-head cockroach Blaberus discoidalis. We tested the model by measuring the maximum force generated in vivo by the hind leg of the cockroach, the coxa–femur joint angle and the position of this leg during a behavior, wedging, that was likely to require maximum torque or moment production. The product of the maximum force of the leg and its moment arm yielded a measured coxa–femur joint moment for wedging behavior. The maximum musculo-apodeme moment predicted by summing all extensor muscle moments in the model was adequate to explain the magnitude of the coxa–femur joint moment produced in vivo by the cockroach and occurred at the same joint angle measured during wedging. Active isometric muscle forces predicted from our model varied by 3.5-fold among muscles and by as much as 70% with joint angle. Sums of active and passive forces varied by less than 3.5% over the entire range of possible joint angles (0–125°). Maximum musculo-apodeme moment arms varied nearly twofold among muscles. Moment arm lengths decreased to zero and switched to the opposite side of the center of rotation at joint angles within the normal range of motion. At large joint angles (>100°), extensors acted as flexors. The effective mechanical advantage (musculo-apodeme moment arm/leg moment arm = 0.10) resulted in the six femoral extensor muscles of the model developing a summed force (1.4 N) equal to over 50 times the body weight. The model’s three major force-producing extensor muscles attained 95% of their maximum force, moment arm and moment at the joint angle used by the animal during wedging.

Key words: locomotion, mechanics, force, arthropods, computer model.

Introduction

Major advances in the study of neural control (Arbas et al. 1995), isolated muscle function (Delcomyn, 1982; Josephson, 1993; Full, 1995) and biomechanics (Full, 1993) illustrate the advantages of investigating arthropod systems. However, integration of locomotor mechanics, neural control and muscle function remains elusive. This integration has been prevented largely because of the complexity of the musculo-skeletal system. The number of variables in even a simple multimuscle system is enormous. Muscular and skeletal parameters can depend on three-dimensional geometry, which further adds to the complexity of this system.

We contend that at least two complementary approaches are required to address the complexity of the musculo-skeletal system. Direct measurements of selected musculo-skeletal parameters are essential and irreplaceable. Equally as important, however, is the creation of a musculo-skeletal model. The model can serve several purposes. It can operate as a hypothesis generator for direct experimentation. Moreover, it can guide direct experimentation by the use of sensitivity analyses to identify the parameters that are most likely to have the greatest effect on performance. Finally, the model can allow estimation of parameter values that are simply too difficult to measure directly.

By presenting a three-dimensional musculo-skeletal model of an insect leg, the present study represents a first step towards integrating information on the mechanics, neural control and musculo-skeletal function in arthropod terrestrial locomotion. We modeled the hind (metathoracic) leg of the death-head cockroach Blaberus discoidalis. We selected this species because more information exists on its biomechanics (Blickhan and Full, 1993; Ting et al. 1994; Full and Tu, 1990; Full et al. 1991; R. Kram, B. Wong and R. J. Full, in preparation) and energetics (Full and Tullis, 1990; Herreid II and Full, 1984) than on any other terrestrial arthropod. We modeled entire musculo-apodeme complexes (MACs; the apodeme is the arthropod equivalent of the tendon) rather than muscles alone.
because musculo-skeletal complex performance has been shown to be affected by series elasticity (Lieber et al. 1992; Zajac, 1989). Our model included direct measurements and estimates of muscle and apodeme parameters for six femoral extensor muscles, the three-dimensional positions of the origins and insertions of these muscles, joint type and range of joint motion (Fig. 1). These structural and functional components allowed us to predict isometric musculo-apodeme complex force ($F_{MAC}$), the MAC moment arm ($r$) and the MAC moment ($M_{MAC}$) or turning force produced at a range of joint angles where:

$$M_{MAC} = F_{MAC} r.\quad (1)$$

We tested our model by examining a near-static behavior, wedging, during which femoral extensor muscles develop isometric force to push the cockroach. We measured the force produced by the hind leg ($F_{Leg}$), the leg moment arm ($R$) and coxa–femur joint angle of an animal wedging through a slot. We compared the maximum coxa–femur joint moment during wedging ($M_{Leg}$) and the coxa–femur joint angle at maximum moment to that predicted by our musculo-skeletal model at that angle (Fig. 2). Since total musculo-apodeme moment ($M_{MAC}^T$, predicted) should equal the leg moment ($M_{Leg}$, measured), we hypothesize that:

$$F_{MAC}^T r = F_{Leg} R \quad (2)$$

$$M_{MAC}^T = M_{Leg} \quad (3)$$

where $F_{MAC}^T$ is the total MAC force and $r$ is the mean MAC moment arm.

Subsequently, we used our model to test hypotheses concerning maximum moment production by MACs and the joint angles at which maximum moment is attained. There is evidence suggesting that musculo-tendon function (Haffajee et al. 1972), joint kinematics (Sale et al. 1982) or both (Lieber and Boakes, 1988) are the major determinants of joint moment. Some studies support the possibility of an optimal joint angle

Fig. 1. Three-dimensional musculo-skeletal model of the ventral view of the metathoracic leg of Blaberus discoidalis. Brown interconnecting lines make up the polygons which represent the exoskeleton. Orange lines represent the lines of action of the muscles. The model is articulated at the coxa/trochanter–femur and femur–tibia joints so that muscle lengths, moment arms, forces and joint moments can be estimated for a range of joint positions. The computer model was created using SIMM (MusculoGraphics Inc., Evanston, IL, USA).
where force production, moment arm and moment are maximized (Ismail and Ranatunga, 1978; Knapik et al. 1983), whereas others find that maximum force production is outside the range of normal motion (Lieber and Boakes, 1988; Sale et al. 1982; Andriacchi et al. 1984). Still other studies point to the utility of a broad distribution of moment as a function of joint angle, which can result when force production and moment arm are each maximized at different joint angles (Hoy et al. 1990).

Using our model for each of the six extensor MACs operating the coxa–femur joint, we tested two hypotheses. First, for each MAC, we determined whether maximum $M^{MAC}$, maximum $F^{MAC}$ and maximum $r$ occur at the same joint angle. Alternatively, MACs could have broad moment distributions. Second, we determined whether the joint angle at the predicted, maximum $M^{MAC}$ for each MAC equals the actual joint angle measured at maximum moment production in the animal during wedging. Alternatively, MACs could be constructed to generate maximum moments at various joint angles.

**Materials and methods**

**Animals**

We used adult death-head cockroaches Blaberus discoidalis (Serville) of both sexes. Cockroaches were housed in plastic containers and given food and water ad libitum. Animals used for morphometric measurements were killed in a jar saturated with ethyl acetate vapor. All dissections and preparations were performed at room temperature (24°C).

**Wedging measurements**

**Kinetics**

Vertical, horizontal and lateral components of the ground reaction forces were measured for cockroaches during wedging by using a miniature force plate (Full and Tu, 1990). We constructed a platform around the force plate, allowing the measurement of forces produced by the hind (metathoracic) leg only (Fig. 2). Animals wedged through a small hole into a darkened box. A sandpaper floor provided the animals with sufficient traction to prevent slippage. We analyzed trials

![Fig. 2. Schematic diagram of leg function during wedging behavior. (A) Ventral view of cockroach on a platform with its metathoracic leg pushing on the force plate (light shaded area). The animal wedged through a slot (heavy shaded area). Leg force on the force plate is represented by a vector (arrow). The bold straight lines represent leg segments and the open circle shows the center of rotation. (B) Equilibrium conditions in the cockroach leg during wedging behavior. Musculo-apodeme complex moment $M^{MAC}$ ($F^{MAC} \cdot \bar{r}$) is assumed to equal the leg moment $M^{Leg}$ ($F^{Leg} \cdot R$). The coxa-femur angle is represented by $\theta$.](image-url)
during which the animal pushed for at least 500 ms and did not slip.

The force plate was constructed of model airplane plywood and mounted on four brass beams which had 24 semiconductor strain gauges bonded to spring blades (Full and Tu, 1990). Force signals were sampled at a frequency of 1000 samples s$^{-1}$. Signals from the force platform were amplified (Vishay, Measurements Group) and collected by an analog-to-digital converter (C-100, Cyborg) interfaced with a computer (IBM PC/AT). Data acquisition and analysis software (Discovery, Cyborg) were used to collect the signals, to filter the data digitally (185 Hz Butterworth filter with zero phase shift) and to make baseline corrections. Loads in the range 0.0001–0.5 N produced a linear response with a maximum variation across the platform of less than 7%. Data were corrected for crosstalk between directions.

**Kinematics**

We videotaped cockroaches wedging through a small hole into a darkened box. To visualize the joint of interest (coxa–femur joint) clearly, we positioned the cameras below the Plexiglas surface. Sandpaper covered the surface in the area of leg contact to prevent slippage, but did not obstruct the camera views of the coxa–femur joint. The coxa and femur segments and the coxa–femur joint were marked with white epoxy paint (Duro Appliance) for digitizing. Two views of the animal were videotaped simultaneously at 1000 frames s$^{-1}$ using high-speed video cameras (Kodak Ektrapro 1000) placed at 90° relative to one another. Direct linear transformation of the data captured in the two view provided the three-dimensional coordinates for the coxa–femur angle of the joints motions, muscle lines of action and muscle force-generating parameters. The mean body mass of animals used for reconstruction was 2.70±0.56 g (S.D.; N=13).

**Musculo-skeletal reconstruction**

The computer model of the insect leg was implemented within a computer program (called SIMM, Software for Interactive Musculoskeletal Modeling; MusculoGraphics, Inc.; Delp et al. 1990; Delp and Loan, 1995). Within the program, a computer model of jointed framework musculo-skeletal structures can be defined by describing the skeletal geometry, joint motions, muscle lines of action and muscle force-generating parameters. The mean body mass of animals used for reconstruction was 2.70±0.56 g (S.D.; N=13).

**Exoskeleton**

**Histology.** Serial reconstruction of sections of the leg segment provided a quantitative description of the exoskeleton. Hind legs were dissected from the body. Leg segments (coxa, trochanter and femur, tibia, tarsus) were separated by cutting the two points of articulation which connect the segments. Subsequently, segments were fixed individually in Bouin’s fluid (Humason, 1979) for 18–24 h. Injection of fixative into each segment ensured complete infiltration and removal of residual air bubbles. Dehydration of the segments was carried out using the n-butanol dehydration sequence shown in Table 1 (R. L. Pipa, personal communication). Each segment was placed in the appropriate alcohol mixture and injected with the solution to ensure complete dehydration.

We embedded segments in paraffin with reference hairs on either side that ran the entire length of the segments. Trimmed tissue blocks were sliced into 80 μm sections using a sledge microtome (AO Spencer Sliding Microtome).

**Computer imaging.** We videotaped the leg segment sections using a video-microscope [Javelin CCTV (chromochip II) video camera; Wild Heerbrugg M7 5 microscope] with a background grid, which served as a calibration scale during image analysis. Image-grabbing hardware (Image Grabber, Neotech Ltd) was used to capture the video images of the sections. The two-dimensional (x,y) coordinates of each section were determined using an image analysis program (Image 1.14u, NIH). Reference hairs that ran parallel to the length of the leg allowed alignment of the sections in the x,y plane. z-axis coordinates were determined by the thickness of the sections (80 μm) and number of sections. Each (x,y,z) coordinate generated a vertex.

We constructed polygons representing the exoskeletal surface by connecting the vertices between consecutive sections (Fig. 1). Not all the sections were incorporated into the model. We used a larger number of sections in areas of muscle attachment than for straighter regions that lacked muscular attachment.

**Joint definition**

Each segment was contained within its own reference frame. The segments were assumed to be articulated by frictionless joints with single degrees of freedom. Cockroach leg segments are mostly connected by simple hinge or pin joints, each with a single axis of rotation. The coxa–trochanter and femur–tibia joints each articulate at only two hinge points. The trochanter–femur joint is also a simple hinge joint (Dresden and Nijenhuis, 1953), but was not included in the model. We assumed that the trochanter–femur joint was unimportant because there was no measurable change in this joint angle. We combined the trochanter and femur segments into a single rigid segment referred to as the ‘femur’. Although the tibia–tarsus joint is complex, having more degrees of freedom, this joint has a very small range of motion. The present study focuses on extension of the femur at the coxa–femur joint and

<table>
<thead>
<tr>
<th>Solution number</th>
<th>Ethanol parts</th>
<th>Ethanol (%)</th>
<th>Absolute n-butanol (parts)</th>
<th>Dehydration time (h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>10</td>
<td>35</td>
<td>0</td>
<td>0.5</td>
</tr>
<tr>
<td>1</td>
<td>9</td>
<td>45</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>8</td>
<td>60</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>6.5</td>
<td>75</td>
<td>3.5</td>
<td>1</td>
</tr>
<tr>
<td>4</td>
<td>4.5</td>
<td>90</td>
<td>5.5</td>
<td>18–24</td>
</tr>
<tr>
<td>5</td>
<td>2.5</td>
<td>90</td>
<td>7.5</td>
<td>18–24</td>
</tr>
<tr>
<td>6</td>
<td>0</td>
<td>0</td>
<td>10</td>
<td>18–24</td>
</tr>
</tbody>
</table>
examines only those joint angles within the normal range of motion in the animal.

**Muscle line of action**

We obtained the three-dimensional coordinates of the muscle attachment points by video microscopy of muscle dissections. Animals were fixed and dehydrated with Kahle’s fluid (Borror and DeLong, 1971) for 4–7 days, after which the metathoracic legs were removed. The origin and insertion points of each MAC were identified on the exoskeleton during dissections. Preparations were moistened with 70% ethanol, as required, to prevent desiccation of the muscles. Muscle attachment points were videotaped at three known viewing angles (20°, 0°, −20°) using a rotating micromanipulator. Although a 90° angle between the video cameras is optimal, all necessary reference and attachment points were not simultaneously visible at larger angles because of the shape of the segments. Direct linear transformation of the data captured in the three views provided the three-dimensional coordinates of the muscle attachment points (Biewener and Full, 1992). An acrylic box (6.78 mm × 6.78 mm × 7.08 mm) served to calibrate the image analysis system (Peak Performance Technologies, Inc.).

Using three predetermined reference points and several anatomical landmarks on the exoskeleton, we rotated and translated the muscle coordinates to match the exoskeletal coordinates. For the current model, we identified 21 musculo-apodeme actuators (notation of Carbonell, 1947). In the present study, we focus on the six femoral extensors relevant to force production during wedging (Fig. 3; Table 2). Although the number of discrete muscles in a cockroach leg is controversial (Alsop, 1978; Becht, 1959; Stokes et al. 1975), we believe our choice represents the major functional groups. In the future, however, actuators may be further differentiated in the model according to other distinguishing features, such as muscle fiber type.

**Moment arm length**

Total musculo-apodeme length (l_{MA}) was determined by summing the length vectors from the origin to the insertion (Delp et al. 1990; Hoy et al. 1990). Musculo-apodeme complexes in the present study required only a single vector because their paths followed only one direction. However, this

---

**Table 2. Femoral extensor musculo-apodeme parameters used in cockroach metathoracic leg model**

<table>
<thead>
<tr>
<th>Extensor muscle</th>
<th>Maximum isometric force, $F_0^M$ (N)</th>
<th>Optimal fiber length, $l_{oM}$ (mm)</th>
<th>Apodeme slack length, $l_{S}^A$ (mm)</th>
<th>Pennation angle, $\alpha$ (degrees)</th>
<th>Normalized apodeme slack length, $l_{S}^M/l_{oM}$</th>
<th>$l_{A}^M$ to moment arm length ratio, $l_{A}^M/l_{r}$</th>
<th>$l_{S}^A$ to moment arm length ratio, $l_{S}^A/l_{r}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>177a</td>
<td>0.28</td>
<td>8.3</td>
<td>4.4</td>
<td>0.0</td>
<td>0.53</td>
<td>10.4</td>
<td>5.5</td>
</tr>
<tr>
<td>177c</td>
<td>0.46</td>
<td>10.3</td>
<td>4.4</td>
<td>0.0</td>
<td>0.42</td>
<td>13.6</td>
<td>5.8</td>
</tr>
<tr>
<td>177d</td>
<td>0.14</td>
<td>3.2</td>
<td>0.6</td>
<td>16.0</td>
<td>0.19</td>
<td>3.5</td>
<td>0.65</td>
</tr>
<tr>
<td>177e</td>
<td>0.14</td>
<td>4.3</td>
<td>0.3</td>
<td>13.0</td>
<td>0.07</td>
<td>5.3</td>
<td>0.37</td>
</tr>
<tr>
<td>178</td>
<td>0.25</td>
<td>2.5</td>
<td>1.3</td>
<td>0.0</td>
<td>0.50</td>
<td>3.3</td>
<td>1.6</td>
</tr>
<tr>
<td>179</td>
<td>0.14</td>
<td>3.3</td>
<td>0.7</td>
<td>0.0</td>
<td>0.20</td>
<td>6.1</td>
<td>1.2</td>
</tr>
</tbody>
</table>

Muscles are numbered following Carbonell (1947).

Optimal muscle fiber length is the fiber length at maximum isometric force production.

Apodeme slack length is the apodeme length beyond which the apodeme begins to develop force.

Moment arm length is at joint angle of maximum force.
Musculo-apodeme moment arm length \( r \) was calculated by the ‘partial velocity’ method, which yields the same results for hinge joints as the cross-product between the vector connecting the joint center to the origin and the unit vector connecting the origin to the insertion (Delp and Loan, 1995).

Musculo-skeletal model

Numerous models of whole muscle function exist (Hatze, 1973; Zajac, 1989; Lieber et al. 1992; van Leeuwen, 1992). We used a Hill-type model of muscle function which incorporated apodeme properties (Zajac, 1989). Each musculo-apodeme actuator was represented by (1) an active contractile element, (2) an elastic element parallel to the contractile element and (3) a passive elastic element in series with the contractile and parallel elastic elements (Delp and Loan, 1995).

The force–length properties of each musculo-apodeme actuator were determined by scaling a dimensionless model. All forces were normalized to maximum isometric force \( (F^M) \). All lengths were normalized to optimal muscle fiber length \( (l^M_o) \) where \( l^M_o \) is the muscle length at which maximum active, isometric force is produced. Normalized isometric muscle force \( (F^M) \) equaled muscle force \( (F^M) \) divided by maximum isometric force \( (F^M) \). Normalized muscle fiber length \( (l^M) \) equaled muscle fiber length \( (l^M) \) divided by optimal muscle fiber length \( (l^M_o) \). The parallel elastic element was set to develop force at \( l^M_o \) and to increase exponentially to a value of \( F^M=2 \) at \( 1.6 l^M_o \) (Hoy et al. 1990).

Apodemes were represented by elastic elements that operated in the linear region of their stress–strain curve. Apodeme cross-sectional area was assumed to be proportional to muscle cross-sectional area and \( F^M \) for each actuator (Zajac, 1989, p. 376). Normalized apodeme force \( (F^A) \) equaled apodeme force divided by \( F^M \). Normalized apodeme length \( (l^A) \) equaled apodeme length \( (l^A) \) divided by \( l^M_o \).

Normalized apodeme force \( (F^A) \) is a function of \( l^A \) and \( F^M \) of muscle fibers adjusted for pennation angle \( (\alpha) \), where \( \alpha \) is the angle between the line of action of the muscle and the direction of the muscle fibers. \( F^A \) is also a function of normalized apodeme stiffness \( (k^A) \) and \( l^A \). Because \( F^A \) is a function of \( l^A \) (\( l^A=F^A \cos\alpha \)), \( F^A \) could be calculated iteratively at each value of \( l^A \) by finding a value of \( F^M \) that satisfies the relationship between \( F^A \) and muscle length and force, as well as the relationship to its own stiffness and length (see equations 5 and 6 in Hoy et al. 1990).

Results from the model were obtained using an interactive computer program (SIMM) on a computer workstation (Silicon Graphics, Personal Iris, 4D25 Super Turbo).

Musculo-skeletal parameters

Muscles

Maximum isometric force \( (F^M) \) for each femoral extensor was estimated by multiplying the maximum isometric stress value of 15 N cm\(^{-2} \) measured directly from experiments on muscle 179 (tetanizing stimulation at 100–200 Hz and two times threshold for the motor axon for 300 ms, R. K. Josephson and D. R. Stokes, unpublished) by our estimates of the physiological cross-sectional area (PCSA) of a muscle (Biewener and Full, 1992). The PCSA for each femoral extensor muscle was determined from the muscle mass, length and density (assuming density of muscle to be 1.056 g cm\(^{-3} \); Mendez and Keys, 1960). To determine muscle mass, the muscles were dissected and weighed on a microbalance. The muscle tissue was moistened with iso-osmotic insect Ringer’s solution, when necessary, and blotted dry just prior to weighing. We measured the joint angle at resting tension in live animals to determine the optimal muscle fiber length \( (l^M_o) \) of each muscle. The fiber length at this resting joint angle was used as the muscle fiber reference length \( (l_{ref}) \). The optimal muscle fiber length was assumed to be 97 % of \( l_{ref} \) on the basis of measurements from the bifunctional muscle of the locust (metathoracic second tergocoxal muscle; Malamud, 1989).

Reference fiber lengths were measured with an electronic digital caliper from the origin on the exoskeleton to the insertion on the apodeme. We used a normalized force–length curve which gave 50 % \( F^M \) at 0.6 \( l^M_o \) and 1.3 \( l^M_o \) (Gordon et al. 1966; Malamud, 1989). Pennation angle \( (\alpha) \) of the muscle fibers was measured with an ocular goniometer mounted on a microscope. Total force of the actuator was the sum of the active force of a muscle and the passive force of the MAC. Muscles were assumed to be fully activated at each joint angle for comparison with maximum isometric contractions used during wedging.

Apodeme

We estimated apodeme slack length (the apodeme length beyond which the apodeme just beings to develop force; \( l_S^A \)) by measuring the length of the apodeme to which the muscles attached. We used a value of 13 GPa for the apodeme’s elastic modulus \( (E^A \) from grasshoppers; Ker, 1977) and 8.6 MPa for its stress \( (\sigma^A; \) determined from our estimates of maximum isometric force and apodeme PCSA). These values gave us the following apodeme stiffness \( (k^A) \) normalized to \( l^M_o \) and \( F^M \) (see Zajac, 1989, p. 377, Fig. 9 for derivation):

\[
k^A = \frac{F^A}{\sigma^A} (1/l_S^A),
\]

\[
k^A = (13 \text{ GPa}/8.6 \text{ MPa}) (1/l_S^A),
\]

\[
k^A = 1500/l_S^A,
\]

where \( l_S^A \) represents the normalized apodeme slack length \( (l_S^A=l^A/l_M^o) \). The value of \( E^A \) was 10 times that of vertebrate tendon values, whereas \( \sigma^A \) was one-quarter of the tendon value (see Hoy et al. 1990). The resulting \( k^A \) was 40-fold stiffer than tendon. We suspect that the value of \( E^A \) may be too high for the cockroach, since the resulting safety factor is so large. However, to our knowledge, the only value available for \( E^A \) is from a specialized jumper, the grasshopper. Fortunately, even when we reduced \( E^A \) by half (6.5 GPa; 20-fold stiffer than tendon), it had no effect on the present results.
Results

Hind leg function during wedging

Force production

While attempting to escape, cockroaches (mean body mass 3.15±0.75 g, s.d.; N=5) pushed, or wedged, through a small slot by the alternate thrusting of the hind (metathoracic) legs. Ground reaction forces generated in the horizontal direction (i.e. along the long body axis of the animal) were greatest in magnitude (Fig. 4). The combination of horizontal and vertical forces directed the resultant force vector along the long axis of the leg when viewed in a lateral projection. Lateral forces were variable, but tended to direct the ground reaction force vector along the tibia through the femur–tibia joint and towards the body axis [8±3° (S.E.M.) relative to the body axis; Fig. 2]. A plateau in the resultant ground reaction force pattern was observed that lasted 100 ms or longer and varied by less than ±10% of the mean value (Fig. 4). The resultant steady-state ground reaction force equal to the magnitude of $F_{LEG}$ was 0.10±0.013 N (S.E.M.; N=5 animals; Table 3). Peak resultant ground reaction forces produced for less than 100 ms were 1.2 times that of steady-state values (Table 3).

Moment arm and moment

The leg or ground reaction force moment arm of the coxa–femur joint ($R$) was approximately 8 mm (Table 3). The product of the leg moment arm ($R$) and the leg force ($F_{LEG}$) yielded the maximum coxa–femur joint moment ($M_{LEG}$). The maximum coxa–femur joint moment ($M_{LEG}$) ranged from 0.80 to 0.96 N mm for steady-state and peak forces, respectively (Table 3).

![Fig. 4. Ground reaction forces of the metathoracic leg during wedging. Forces for three components are shown along with their resultant over time. The steady-state resultant force is shown in the shaded column. The calculation of maximum leg moment ($M_{LEG}$) incorporated the leg force ($F_{LEG}$) which equals the magnitude of the ground reaction force vector resolved in the plane of the leg.](image)

| Table 3. Comparison of coxa–femur joint properties at maximum moment derived from the femoral extensor musculo-apodeme model with direct measurements from leg ground reaction forces during wedging |
|---|---|---|---|
| Source | Force (N) | Effective moment arm (mm) | Moment (N mm) | Coxa–femur angle (degrees) |
| Animal in vivo leg measurements | $F_{LEG}$ | $R$ | $M_{LEG}$ | |
| Steady-state force | 0.10±0.013 | 8.0±1.82 | 0.80 | 45±4.9 |
| Peak force | 0.12±0.019 | 8.0±1.82 | 0.96 | 45±4.9 |
| Model | $F_{MAC}$ | $r$ | $M_{MAC}$ | |
| Musculo-apodeme | 1.4 | 0.86 | 1.20 | 43–47 |

Values are means ± 1 S.E.M.
Joint angle

The coxa–femur joint angle of the metathoracic leg during wedging was 45±4.9° (S.E.M.; N=6; Table 3).

Musculo-apodeme model

Musculo-apodeme complex parameters

Maximum isometric force ($F^\text{OM}$) estimates for the six extensor muscles ranged from 0.14 to 0.46 N (3.5-fold variation; mean 0.24±0.13 N, s.d.; Table 2). Optimal muscle fiber lengths ($l^\text{OM}$) for the six extensors varied by fourfold (mean 5.3±3.2 mm, s.d.). By far the longest fibers were those of the bifunctional muscles 177a and 177c. Apodeme slack length ($l^\text{SA}$) varied 15-fold (mean 1.95±1.93 mm, s.d.) among extensors. Only muscles 177d and 177e had significant pennation angles (Table 2).

Active muscle force

Active isometric muscle force varied significantly among muscles (Fig. 5A). Maximum isometric force was attained for all muscles at coxa–femur joint angles greater than 75°. At joint angles less than 75°, active force declined from 16 to 70 % for four of the six muscles. The two longest muscles (177a, 177c) showed no reduction in force as the joint angle decreased.

Passive muscle force

Musculo-apodeme complex passive force varied among muscles and as a function of joint angle (Fig. 5B). Passive force increased for all muscles at joint angles less than 50°. Passive force was small for muscles 177a, 177c and 179. Muscle 177e made the largest passive contribution; two-thirds of its total force was passive at a 3° joint angle. Passive force of muscles 178 and 177d supplied 15 and 20 % of their total force at a joint angle of 25°, respectively. At small joint angles (<50°), passive force contributed approximately 3–18 % of the total MAC force from all muscles.

Musculo-apodeme complex isometric force

Musculo-apodeme complex isometric force ($F^\text{MAC}$) varied significantly among MACs (Fig. 6A). When active and passive forces are summed, near-maximal isometric force was attained for all MACs over most of the range of coxa–femur joint angles investigated (see Table 2; Fig. 6A). The maximum decrease in active plus passive force ($F^\text{MAC}$) ranged from 4 to 15.5 % for individual muscles and was only 3.5 % for the summed force of all MACs.

Musculo-apodeme complex moment arm

Maximum MAC moment arm varied among MACs (0.57–1.00 mm; mean 0.86±0.17 mm, s.d., N=6), but to a far lesser extent than force production (Fig. 6B). Most of the variation in moment arm was explained by joint angle. The mean joint angle at which MACs attained maximum moment arm was 44±13.5° (s.d.). Moment arm decreased by 7–46 % at the smallest joint angle (3°). Large joint angles, associated with extension of the femur, produced substantial decreases in moment arm for all MACs. At joint angles greater than 100°, moment arm decreased to below zero and changed to the opposite side of the center of rotation.

Musculo-apodeme complex moment

Musculo-apodeme complex moment varied substantially among muscles and as a function of joint angle (Fig. 6C). The mean joint angle at which muscles attained maximum moment was 48.5±15.1° (s.d.). For individual muscles, moment decreased by 15–50 % at the smallest joint angle (3°) and by 18 to over 80 % at 100°. At angles greater than 100°, moment was negative, producing flexion rather than extension.

The maximum summed moment from all muscles collectively ($M^\text{MAC}_T$) was 1.2 N mm at a joint angle of 45° (Table 3; Fig. 7).
Insect leg model

Discussion

Wedging

The resultant ground reaction force of the cockroach hind (metathoracic) leg during wedging was nearly 10-fold greater than that measured for the same leg during rapid running (0.013 N; Full et al. 1991). We suspect that this represents maximum force and moment production because these forces are comparable to those that B. discoidalis generates during an emergency behavior, righting, where it must turn over after being flipped onto its dorsal surface (Full et al. 1995).

The ground reaction force of the cockroach leg during wedging was more than fourfold greater than body weight (0.0319 ± 0.0088 N, s.d., N = 5). Alexander (1985) found that force production ranged from 3.7 to 147 times body weight for animals with the mass of cockroaches. He noted that insects fell at the lower end of this distribution and hypothesized a disadvantage for force generation as a result of small muscle moment arms constrained by a narrow, tubular exoskeleton. In the present study, we found that the extensor MACs must generate about ten times as much force ($F_{\text{MAC}}$) as the animal achieves at the distal end of the leg ($F_{\text{Leg}}$; Fig. 2). This difference resulted from the leg force moment arm ($R$) being ten times as long as the musculo-apodeme moment arm ($r$; Table 3). MAC moment arms are short in insects, but are also quite short in small mammals compared with large mammals. The moment arm ratio, or mechanical advantage ($r/R$), of a mouse is only about one-tenth that of a horse (Biewener, 1989). Extrapolation of the scaling of mammalian mechanical advantage (Biewener, 1989) to an animal the size of a cockroach gives a predicted mechanical advantage of 0.05 (Fig. 8). At least for the death-head cockroach B. discoidalis, the moment arm ratio of 0.1, albeit small, is actually larger than predicted for an animal of its mass. Mechanical advantage calculated for slow, strong dung beetles ranges from 0.06 to 0.13 (Evans and Forsythe, 1984). Fast-running tiger beetles have lower ratios of approximately 0.03. Overall, insect exoskeletons may not necessarily constrain the musculo-apodeme moment arm length.

Death-head cockroaches do not appear to be exceptionally strong pushers or wedgers, at least compared with other insects, such as beetles (Forsythe, 1983). B. discoidalis can be characterized as a moderately strong force producer (force ratio = 2.4–4.8, where force ratio is maximum force/mass$^{0.33}$) and a relatively fast runner (velocity ratio = 2, where velocity ratio is maximum velocity/mass$^{0.33}$; Evans and Forsythe, 1984; Full and Tu, 1990; Forsythe, 1991; Evans, 1977). This cockroach species may fall into the force/speed specialist category used...
to categorize beetles rather than being more specialized for either force- or velocity-dependent activities alone (Evans and Forsythe, 1984).

Musculo-apodeme complex force production

The magnitude of active isometric muscle force predicted from our model varied significantly among muscles due to variation in physiological cross-sectional area (Fig. 5A). We used a muscle stress of 15 N cm$^{-2}$ measured directly from muscle 179 (R. K. Josephson and D. R. Stokes, unpublished). This value is within the range of maximum isometric stresses reported for other invertebrate species (2–140 N cm$^{-2}$; Full, 1995; Ruegg, 1968; Alexander, 1985), amphibians and lizards (7.1–39.6 N cm$^{-2}$; Josephson, 1993) and mammals (13.2–29.4 N cm$^{-2}$; Josephson, 1993; Powell et al., 1984; Close, 1972). Nonetheless, our muscle stress value for the larger, slower, death-head cockroach is approximately twice that found in the smaller, faster American cockroach Periplaneta americana (6.8–8.3 N cm$^{-2}$ for four of six muscles; Smit et al., 1967; Jahromi and Atwood, 1969). Stress may even vary among extensor muscles, since sarcomere length has been shown to vary by twofold in the American cockroach (Stokes, 1987; Fourtner, 1978) and longer sarcomeres with longer myosin filaments will be capable of generating greater stress. Moreover, measurement of maximum isometric force using neural activation could be complicated by facilitation and defacilitation of synaptic effects as well as by circulating hormones. Active isometric force measurements obviously deserve more attention in the future.

Active isometric force varied as a function of joint angle in our model (Fig. 5A). Over most joint angles, the two longest muscles (177a, 177c) operated over the plateau of their force–length curve. These bifunctional muscles, which participate in running and flying, showed only a small decrease in active force production at angles greater than 30–60° because they began to function on the ascending region of the force–length curve. By contrast, the other muscles (177d, 177e, 178, 179) operated on the plateau of the force–length curve at joint angles greater than 75°. Active force decreased considerably at small joint angles (<75°), because these extensor muscles functioned on the descending portion of the force–length curve as they became stretched. The ratio of $l_{0M}/r$ can be an excellent predictor of the range of joint angles over which muscles will develop active force (Hoy et al., 1990; Delp et al., 1990; Zajac, 1989). Large $l_{0M}/r$ ratios, such as in muscles 177a and 177c, resulted in the actuators developing active force over a greater range of joint angles compared with those with smaller ratios, such as muscle 178 (Table 2; Fig. 5A).

Passive force contributed 3–18 % of the total force at joint angles less than 50° (Fig. 5B). At small coxa–femur joint angles, muscles operated on the descending region of the force–length curve. In this region, passive forces increased and offset the decline in active force. For cockroach femoral extensors, the sum of active and passive force resulted in a total musculo-apodeme force that varied by less than 3.5 % over the entire range of possible joint angles (Fig. 6A). Although the maximum $F_{MAC}$ was not produced at the joint angle used by the animal during wedging for any single MAC, the range of angles over which 95 % of the maximum force was generated did include the angle measured in vivo for five of a possible six muscles, including the three muscles producing the greatest force (177a, 177c and 178; Fig. 9).

Estimates of passive force contribution were based on a number of assumptions. First, we estimated that the Young’s modulus ($E^A$) of a cockroach apodeme was comparable to that measured in the locust, and that the complex was functioning over the linear portion of the apodeme stress–strain curve. Lieber et al. (1991) found that frog semitendinosus muscle can operate in the ‘toe’ region of the stress–strain curve where stiffness increases with load. Moreover, the elastic modulus of the frog tendon was one-tenth of that of most mammalian tendons, reinforcing our concern regarding variability in apodeme/tendon properties. To limit the number of variables in the model, we assumed that apodeme cross-sectional area was proportional to muscle PCSA or to $F_M^A$ (Hoy et al., 1990). Our preliminary estimates supported this assumption, although cases where muscles attach to the same apodeme need to be examined more extensively. Second, we assumed that the passive, parallel elastic element had a normalized force–length relationship similar to that found in locust flight muscle and frog muscle (Malamud, 1989). With this assumption, we may have overestimated our small passive force contribution, because we did not consider heterogeneous fiber lengths that would produce smaller changes in normalized force with a relative length change. We also did not include an adjustment for the transient changes in the tension of stretched or shortened muscle (i.e.
stress relaxation) that have been demonstrated in locust flight muscle (Malamud, 1989) as well as in vertebrate muscle (Buchthal et al., 1944). At present we cannot evaluate the relevance of stress relaxation, other than to say that it has a long time constant and that the largest absolute changes in force occur after relatively large changes in length (e.g. 29%; Malamud, 1989). Finally, for simplicity, the model did not include a muscle elastic or damping component in series with the contractile element, since its inclusion can decouple the relationship between sarcomere length and fiber length (Zajac, 1989). To test the significance of these assumptions, we have begun sensitivity analyses of the effects of changing optimal muscle fiber length, apodeme slack length, Young’s modulus and the parallel elastic component on maximum force, moment and the joint angle at which they are attained (Ahn et al., 1992).

The variation in active isometric force production with joint angle is dependent on the optimal muscle fiber length, apodeme slack length and the shape of the normalized force–length curve. The width of the force–length curve is known to vary substantially among invertebrates (Full, 1995). Flight muscle in insects operates over a very narrow strain range (50% maximum isometric force at ±3% strain), whereas the muscles of hydrostatic animals can have a very broad range (50% maximum isometric force at ±50% strain). Our force–length curve fell between these two extremes (50% maximum isometric force at ±30–35% strain), but obtaining force–length curves for cockroach extensors should be a priority in the near future. Alteration in the MAC force–length relationship is best characterized by the ratio of apodeme slack length to optimal muscle fiber length ($l_{SA}/l_{OM}$). Compliant musculo-tendon actuators have ratios greater than 1, which widen the ascending region of the force–length curve as well as increase the relative muscle length at which maximum force is attained (Zajac, 1989; Hoy et al., 1990). Values of $l_{SA}/l_{OM}$ range from 0.01 (gluteus maximus) to 11.3 (soleus) in humans (Hoy et al., 1990), and from 1 (semitendinosus) to 6 (plantarflexors) in cats (Zajac, 1989). The $l_{SA}/l_{OM}$ ratio of the semitendinosus muscle of frogs is 1.5 (Lieber et al., 1991). By comparison, cockroach extensor musculo-apodeme actuators appear relatively stiff ($l_{SA}/l_{OM}$ = 0.07–0.53; Table 2), so that changes in active force should result largely from shifts on the muscle fiber force–length curve.

**Musculo-apodeme complex moment arm**

Maximum moment arm varied by nearly twofold among muscles, but was far more sensitive to joint angle (Fig. 6B). The model’s predictions of joint moment are striking because moment decreased to zero and switched to the opposite side of the center of rotation at joint angles within the normal range of motion. Certainly, the effect of the action of the muscle on leg function cannot be assessed without exoskeletal morphological data, even if the musculo-apodeme force is known. MAC moment arms resulted in the extensor muscles of the metathoracic leg developing a total force equivalent to over 50 times body weight to generate the leg ground reaction force measured. The force summed from all the MACs in the cockroach hind leg coxa was approximately 10 times greater than the force output at the leg due to the moment arm ratio ($r/R$). These estimates are only for the case where moment arm is maximal. The summed MAC force would have to double to 100-fold the body weight to exert the same leg ground reaction force if the joint angle was increased from 45 to 100°.
All moment arm lengths were within 5% of the maximum at the in vivo joint angle used by the animal during wedging (Fig. 9). In particular, the joint angles at which maximum moment arm was produced for the three major moment-generating muscles (177c, 177a and 178) were remarkably close to the joint angle used during wedging behavior.

Musculo-apodeme complex moment

The total MAC moment (\(M_{\text{MAC}}\)) predicted by the model adequately explained the joint moment measured in a wedging cockroach (\(M_{\text{Leg}}\)). The data lend support to the parameter values used in the model because predicted musculo-apodeme moment (\(M_{\text{MAC}}\)) was similar to the measured leg moment (\(M_{\text{Leg}}\)). \(M_{\text{MAC}}\) was only 30–50% greater than the value determined from ground reaction force data (Table 3). Note that the moment determined from the ground reaction force (\(M_{\text{Leg}}\)) is a net moment (extensor – flexor), whereas the model-generated moment was based solely on the extensor muscle moment production. Therefore, any flexor contribution to the moment would tend to make the moment values of the model closer to that measured during wedging. Moreover, all extensor muscles may not be fully active in the animal during wedging.

MAC moment was determined by both musculo-apodeme force production and joint kinematics. Musculo-apodeme force, and to a lesser extent moment arm, set the magnitude of the maximum moment. The variation in moment with joint angle resulted almost exclusively from the variation in moment arm (Fig. 6). MACs with large moment arms can generate larger moments. However, large moment arms cause MACs to go through greater excursions with changes in joint angle, thereby limiting the range of joint angles over which moment is developed (Delp and Zajac, 1992). The moment arm length of muscle 179 was three-fifths of that of muscle 177d. Correspondingly, the maximum active moment produced by muscle 179 was three-fifths of that of muscle 177d. However, muscle 179 developed 80% of its maximum active moment over a 10° wider range of joint angles than muscle 177d because of its smaller excitations with changes in joint angle. These results further support the conclusion that isolated muscle function alone simply cannot predict joint and leg function. Perhaps the most extreme example occurred at coxa–femur angles greater than 100°, where so-called ‘extensors’ acted as flexors to rotate the leg away from its maximum extension (Fig. 6C).

The angle at maximum moment for each individual muscle differed from the joint angle used by the animal during wedging (Fig. 9). Likewise, the joint angles at maximum moment, moment arm and force production did not coincide exactly. Upon first examination, these results appear consistent with the conclusions from studies of human (Hoy et al. 1990) and frog (Lieber and Boakes, 1988) leg muscles, where variation in the joint angle of maximum moment arm and force production led to moment production over a broader range of angles. However, the total, maximum MAC moment predicted (\(M_{\text{MAC}}\)) by the present model did occur at the same joint angle (45°) measured in the animal during wedging (Table 3). Furthermore, all musculo-apodeme moments at the in vivo joint angle were within 15% of the maximum and five out of the six muscles were within 5%. In particular, the joint angles at maximum moment for all three major moment-generating muscles (177c, 177a and 178) were remarkably close to the joint angle used by the animal during wedging (Fig. 9). With the single exception of muscle 177e, the joint angle ranges representing 95% of maximum values for moment arm length and force production overlapped with each other, with the joint angle range representing 95% of maximum moment and with the angle used in vivo during wedging.

The present musculo-skeletal model supports design hypotheses that favor maximum moment production by leg muscles as opposed to the development of smaller moments over a broad range of joint angles. We were surprised that the angle at maximum force, moment arm and moment for the cockroach extensor musculo-apodeme complexes fell, in most cases, within 5% of the maximum, given the estimations made and the assumptions of the model. We are encouraged by the concordance of the model’s predictions and the in vivo measurements on the animal. Sensitivity analyses using the present model with this and other closely related species, in concert with direct measurements, will allow us to answer mechanistic questions of musculo-skeletal function as well as to begin to explore evolutionary hypotheses.

**List of symbols**

- \(\sigma_0^A\) optimal apodeme stress
- \(\alpha\) pennation angle or the angle between the line of action of the muscle and the direction of the muscle fiber
- \(E^A\) elastic or Young’s modulus of apodeme
- \(F^A\) apodeme force
- \(\hat{F}^A\) normalized apodeme force (\(\hat{F}^A = F^A/F^M\))
- \(F_{\text{Leg}}\) resultant, steady-state force by hind leg measured during wedging
- \(F^M\) muscle force
- \(F^M_\text{norm}\) normalized isometric muscle force (\(F^M_\text{norm} = F^M/F^M_\text{max}\))
- \(F_{\text{MAC}}\) musculo-apodeme complex force
- \(F_{\text{MAC}}^{\text{MAC}}\) total musculo-apodeme complex force summed for all muscles
- \(F_{\text{MAC}}^0\) isometric force
- \(\hat{F}^A\) normalized apodeme stiffness
- \(l^A\) apodeme length
- \(l^A_\text{norm}\) normalized apodeme length (\(l^A_\text{norm} = l^A/l^A_\text{opt}\))
- \(l^A_\text{slack}\) apodeme slack length or the apodeme length beyond which the apodeme just begins to develop force
- \(l^M\) muscle fiber length
- \(l^M_\text{norm}\) normalized muscle fiber length (\(l^M_\text{norm} = l^M/l^M_\text{opt}\))
- \(l^M_\text{opt}\) optimal muscle fiber length or the muscle length at which maximum active, isometric force is produced


\[ \text{\( \bar{I}_{\text{MA}} \)} \text{ musculo-apodeme length} \\
\[ \text{\( \bar{I}_{\text{MAC}} \)} \text{ normalized muscle-apodeme length (\( \bar{I}_{\text{MA}} = \text{\( I_{\text{MA}} \)} / \text{\( M \)} \))} \\
\[ \text{\( I_{\text{ef}} \)} \text{ muscle fiber reference length} \\
\[ \text{\( \text{MAC} \)} \text{ musculo-apodeme complex} \\
\[ \text{\( M_{\text{MAC}} \)} \text{ maximum coxa–femur joint moment measured during wedging} \\
\[ \text{\( M_{\text{T MAC}} \)} \text{ total musculo-apodeme complex moment summed for all MACs} \\
\[ \text{PCSA} \text{ physiological cross-sectional area} \\
\[ \text{\( R \)} \text{ leg or ground reaction force moment arm of the coxa–femur joint} \\
\[ \text{\( r \)} \text{ musculo-apodeme moment arm length} \\
\[ \text{\( \tilde{r} \)} \text{ mean MAC moment arm length} \\
\[ \text{\( r/R \)} \text{ moment arm ratio or mechanical advantage} \\
\[ \text{SIMM} \text{ Software for Interactive Musculoskeletal Modeling, MusculoGraphics, Inc.} \\
\]

We thank Scott Delp, Peter Loan, Marvaley Wake, Rudy Pipa, Chris Eckel, Kay Earls, Randi Weinstein, Darrell Stokes, Ben Wong, Rodger Kram, Liz Queatham, Claire Farley and Paul-Henri Arnaud. This work was supported by NSF PYI Grant DCB 90-58138 to R.J.F.

References


relationship of muculotendon actuators at the hip, knee and ankle. 


